

ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ
Γ' ΤΑΞΗΣ ΗΜΕΡΗΣΙΟΥ ΓΕΝΙΚΟΥ ΛΥΚΕΙΟΥ
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ΕΞΕΤΑΖΟΜΕΝΟ ΜΑΘΗΜΑ:
ΦΥΣΙΚΗ ΠΡΟΣΑΝΑΤΟΛΙΣΜΟΥ

ΕΝΔΕΙΚΤΙΚΕΣ ΑΠΑΝΤΗΣΕΙΣ ΘΕΜΑΤΩΝ

ΘΕΜΑ Α

- A1. γ
A2. δ
A3. α
A4. δ
A5. α) Λάθος β) Σωστό γ) Λάθος δ) Σωστό ε) Λάθος

ΘΕΜΑ Β

B1. $d_2 = \sqrt{4\lambda_1^2 + \frac{9\lambda_1^2}{4}} = \sqrt{\frac{25\lambda_1^2}{4}} = \frac{5\lambda_1}{2} = 2,5\lambda_1$

$d_2 - d_1 = 2,5\lambda_1 - \lambda_1 = \frac{\lambda_1}{2}$

$A' = \left| 2A \sin \pi \frac{d_2 - d_1}{\lambda_2} \right| = \left| 2A \sin \pi \frac{\frac{\lambda_1}{2}}{\frac{\lambda_1}{2}} \right| = 2A$

Επιλέγω (i)

B2. $\Sigma \vec{\tau}_{\epsilon\varsigma} = 0 \rightarrow \vec{L}_1 = \vec{L}_2 \rightarrow m u_1 R = m u_2 \frac{R}{2} \rightarrow u_2 = 2u_1$

$W_F = K_2 - K_1 = \frac{1}{2} m u_2^2 - \frac{1}{2} m u_1^2$

$= \frac{1}{2} m (4u_1^2 - u_1^2)$

$= \frac{3}{2} m u_1^2$

$= \frac{3}{2} m \omega^2 R^2$

Επιλέγω (iii)

B3. $x = u_{\Delta} \cdot t$

$$4h = u_{\Delta} \cdot \sqrt{\frac{2h}{g}} \rightarrow 16h^{\frac{3}{2}} = u_{\Delta}^2 \cdot \frac{2h}{g} \rightarrow u_{\Delta} = \sqrt{8gh}$$

Εξ. συνέχειας:

$$\begin{aligned} \Pi_r = \Pi_{\Delta} &\rightarrow A_r \cdot U_r = A_{\Delta} \cdot U_{\Delta} \rightarrow 2A_{\Delta} \cdot U_r = A_{\Delta} \cdot U_{\Delta} \\ &\rightarrow U_{\Delta} = 2U_r \rightarrow \sqrt{8gh} = 2U_r \\ 8gh &= 4U_r^2 \\ gh &= \frac{U_r^2}{2} \end{aligned}$$

Εξ. Bernoulli:

$$\begin{aligned} P_r + \frac{1}{2}\rho U_r^2 &= P_{\Delta} + \frac{1}{2}\rho U_{\Delta}^2 + \rho gh \\ P_r - P_{\Delta} &= \frac{1}{2}\rho U_{\Delta}^2 - \frac{1}{2}\rho U_r^2 + \rho gh \\ &= \frac{1}{2}\rho 4U_r^2 - \frac{1}{2}\rho U_r^2 + \rho \cdot \frac{U_r^2}{2} \\ &= 2\rho U_r^2 \end{aligned}$$

Επιλέγω (i)

ΘΕΜΑ Γ

Γ1. $u_1 = u_{\max} = \omega_1 \cdot A_1$

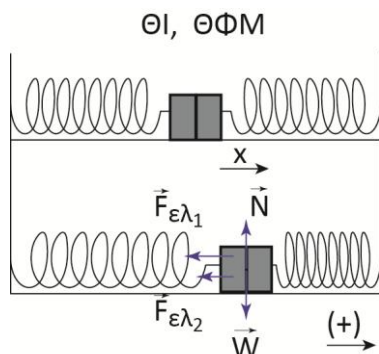
$$= \sqrt{\frac{K_1}{m_1}} \cdot \Delta \ell = 5 \cdot 0,4 = 2 \text{ m/sec}$$

$$\text{ΑΟΔ } \vec{P}_{\alpha\rho\chi} = \vec{P}_{\tau\epsilon\lambda} \rightarrow m_1 \cdot u_1 = (m_1 + m_2) \cdot u_2$$

$$v_z = \frac{u_1}{2} = 1 \text{ m/sec}$$

$$\left. \begin{aligned} f_1 &= \frac{u_{nx} - u_1}{u_{nx}} \cdot f_1 \\ f_2 &= \frac{u_{nx} - u_z}{u_{nx}} \cdot f_2 \end{aligned} \right\} \begin{aligned} f_1 &= \frac{u_{nx} - u_1}{u_{nx}} = \frac{338}{339} \\ f_2 &= \frac{u_{nx} - u_z}{u_{nx}} = \frac{338}{339} \end{aligned}$$

Γ2.



Στη Θ.Ι. $\Sigma F = 0$ (Θ.Φ.Μ)

Σε τυχαία θέση που απέχει x από τη Θ.Ι

$$\Sigma F = -F_{\varepsilon\lambda_1} - F_{\varepsilon\lambda_2}$$

$$\Sigma F = -k_1 \cdot x - k_2 \cdot x$$

$$\Sigma F = -(k_1 + k_2) \cdot x$$

$$\Sigma F = -2k \cdot x$$

Άρα εκτελεί απλή αρμονική ταλάντωση με $D = 2k = 100 \text{ N/m}$.

$$\text{Θ.Ι. } v_z = v_{\max} \rightarrow v_z = \omega \cdot A \rightarrow v_z = \sqrt{\frac{D}{m_1 + m_2}} \cdot A \rightarrow A = 0,2 \text{ m}$$

Γ3. Όταν $v_A = 0$ δηλαδή όταν $x = +A$ για 1^η φορά $f_A = f_s$

Αυτό θα συμβεί $\Delta t = \frac{T}{4}$ μετά την κρούση (Θ.Ι)

$$T = 2\pi \sqrt{\frac{m_1 + m_2}{D}} = 0,4\pi \text{ sec}$$

$$\Delta t = \frac{T}{4} = 0,1\pi \text{ sec}$$

Γ4. $\frac{\Delta P}{\Delta t} = \Sigma F = -D \cdot x$

$$\left| \frac{\Delta P}{\Delta t} \right|_{\max} = D \cdot A$$

$$= 100 \cdot 0,2$$

$$= 20 \text{ kg m/sec}^2$$

ΘΕΜΑ Δ

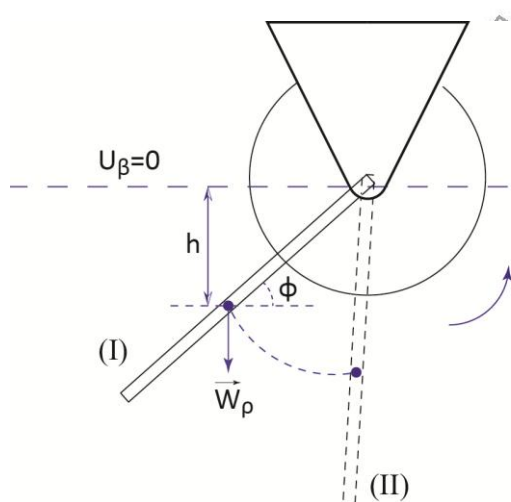
Δ1. Steiner: $I_p^{(0)} = I_{cm} + M\left(\frac{\ell}{2}\right)^2 = \frac{1}{12}M\ell^2 + \frac{M\ell^2}{4} = \frac{1}{3}M\ell^2$

$$\begin{aligned} I_{p-\Delta}^{(0)} &= I_p^{(0)} + I_1^{(0)} = \frac{1}{3}M\ell^2 + \frac{1}{2}m_\Delta R_\Delta^2 \\ &= (24 + 1)\text{kgm}^2 \\ &= 25\text{kgm}^2 \end{aligned}$$

Δ2. $\frac{\Delta \vec{L}}{\Delta t}(\rho - \Delta) = \vec{\Sigma} \tau_{\epsilon\xi} \rightarrow$

$$\begin{aligned} \frac{\Delta L}{\Delta t}(\rho - \Delta) &= W\rho \cdot \frac{\ell}{2} \cdot \sin\phi \\ &= Mg \cdot \frac{\ell}{2} \cdot \sin\phi \\ &= 72\text{kg m}^2 / \text{sec}^2 \end{aligned}$$

Δ3.



ΑΔΜΕ (I) $\rightarrow$ (II)

$$k_{\text{αρχ}} + U_{\text{αρχ}} = k_{\text{τελ}} + U_{\text{τελ}}$$

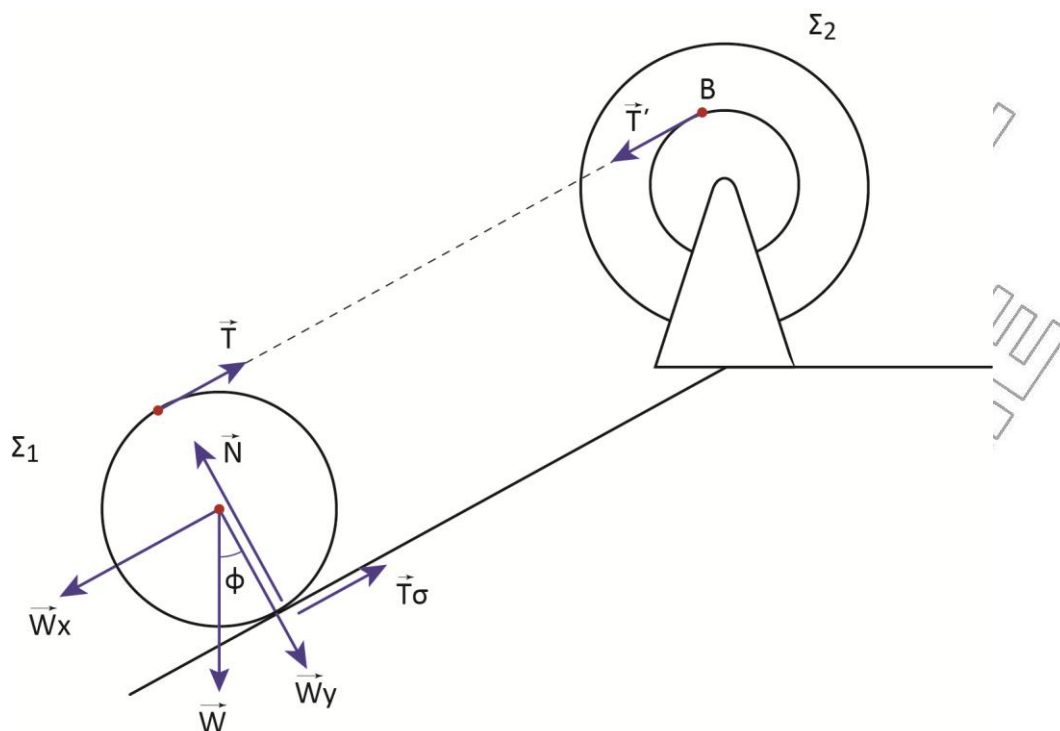
$$-Mgh = k_{\text{τελ}} - Mg\frac{\ell}{2}$$

$$k_{\text{τελ}} = Mg\frac{\ell}{2} - Mgh \quad \text{όπου } h = \frac{\ell}{2}\eta\mu\phi$$

$$k_{\text{τελ}} = Mg\frac{\ell}{2}(1 - \eta\mu\phi)$$

$$k_{\text{τελ}} = 24\text{J}$$

Δ4.



$$v_{cm} = \omega_2 R \rightarrow$$

$$\alpha_{cm} = \alpha_{\gamma\omega v_2} \cdot R$$

$$v_A = 2v_{cm}$$

$$v_A = v_B$$

$$2v_{cm} = v_B$$

$$2v_{cm} = \omega_1 \cdot R$$

$$2 \cdot \alpha_{cm} = \alpha_{\gamma\omega v_1} \cdot R$$

και $T = T'$ (αβαρές νήμα)

$$\Sigma 1. \quad \Sigma \tau = I_{cm} \cdot \alpha_{\gamma\omega v_1} \rightarrow T \cdot R = I_{cm} \cdot \alpha_{\gamma\omega v_1}$$

$$\rightarrow T = \frac{I_{cm}}{R} \cdot \alpha_{\gamma\omega v_1} \quad (1)$$

Σ2.

$$\Sigma F_x = m \cdot \alpha_{cm} \rightarrow W_x - T - T\sigma = m \alpha_{cm}$$

$$\Sigma \tau = I_k \cdot \alpha_{\gamma\omega v_2} \rightarrow T\sigma \cdot R - T \cdot R = \frac{1}{2} m R^2 \cdot \frac{\alpha_{cm}}{R} \quad \left. \vphantom{\Sigma \tau = I_k \cdot \alpha_{\gamma\omega v_2}} \right\} \xrightarrow{(+)}$$

$$\rightarrow Wx - 2T = \frac{3}{2} m \alpha_{cm}$$

$$\stackrel{(1)}{\rightarrow} m g \eta \mu \phi - 2 \cdot \frac{I_{cm}}{R} \cdot \alpha_{\gamma \omega \nu_1} = \frac{3}{2} m \alpha_{cm}$$

$$\rightarrow m g \eta \mu \phi - 2 \cdot \frac{I}{R} \cdot \frac{2 \alpha_{cm}}{R} = \frac{3}{2} m \alpha_{cm}$$

$$\rightarrow \alpha_{cm} = 1 \text{ m/sec}^2$$

$$v_{cm} = \alpha_{cm} \cdot t \rightarrow t = \frac{v_{cm}}{\alpha_{cm}}$$

$$S = \frac{1}{2} \alpha_{cm} \cdot t^2$$

$$S = \frac{1}{2} \alpha_{cm} \cdot \frac{v_{cm}^2}{\alpha_{cm}^2}$$

$$v_{cm} = \sqrt{2 \alpha_{cm} \cdot S} = 2 \text{ m/sec}$$

ΚΑΛΑ ΑΠΟΤΕΛΕΣΜΑΤΑ!!!