

**ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ
ΗΜΕΡΗΣΙΩΝ & ΕΣΠΕΡΙΝΩΝ ΓΕΝΙΚΩΝ ΛΥΚΕΙΩΝ
ΠΑΡΑΣΚΕΥΗ 10 ΙΟΥΝΙΟΥ 2022
ΕΞΕΤΑΖΟΜΕΝΟ ΜΑΘΗΜΑ
ΦΥΣΙΚΗ ΠΡΟΣΑΝΑΤΟΛΙΣΜΟΥ**

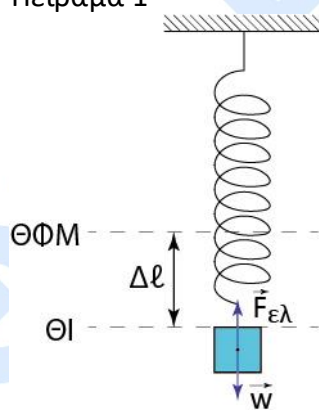
ΕΝΔΕΙΚΤΙΚΕΣ ΑΠΑΝΤΗΣΕΙΣ

ΘΕΜΑ Α

- A1. γ
A2. δ
A3. γ
A4. β
A5. α Λάθος
β. Σωστό
γ. Λάθος
δ. Σωστό
ε. Σωστό

ΘΕΜΑ Β

- B1. Πείραμα 1

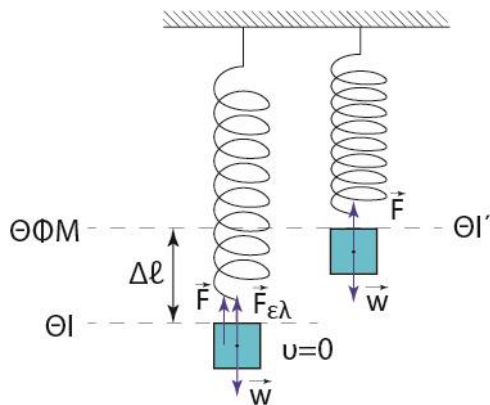


$$\Theta\text{Ι: } \Sigma F = 0 \rightarrow F_{\epsilon\lambda} = w$$

$$k\Delta\ell = mg \rightarrow \Delta\ell = \frac{mg}{k}$$

Στη ΘΦΜ αφήνεται ελεύθερο ($v = 0$) συνεπώς

$$A_1 = \Delta\ell = \frac{mg}{k}$$

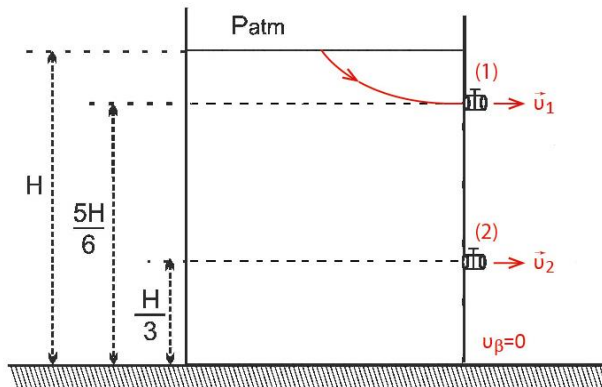


$F = mg$ συνεπώς το σώμα εκτελεί Α.Α.Τ. γύρω από νέα $\Theta Ι'$ που είναι η $\Theta\Phi\text{M}$ αφού έχει $F_{ελ} = 0$ και $\Sigma F = F - mg = 0$.

Η αρχική θέση ισορροπίας είναι ακραία θέση ($u = 0$) και $A_2 = \Delta\ell = \frac{mg}{k}$

Δηλαδή $A_1 = A_2$ (I)

B2.



Εφόσον το εμβαδόν στις οπές είναι αμελητέο σε σχέση με το εμβαδόν του δοχείου, η ταχύτητα της στάθμης του δοχείου είναι μηδενική.

Εξ. Bernoulli $A \rightarrow (1)$

$$P_A + \rho g H = P_1 + \frac{1}{2} \rho u_1^2 + \rho g \frac{5H}{6}$$

$$P_{atm} + \rho g \frac{H}{6} = P_{atm} + \frac{1}{2} \rho u_1^2 \rightarrow u_1 = \sqrt{\frac{gH}{3}}$$

όμοια

$$u_2 = 2 \cdot \sqrt{\frac{gH}{3}} = 2u_1$$

$$\Pi_1 = A \cdot u_1 \rightarrow \frac{v}{\Delta t_1} = A \cdot u_1 \rightarrow \Delta t_1 = \frac{v}{A \cdot u_1}$$

$$\Pi_1 + \Pi_2 = A \cdot u_1 + A \cdot u_2 \rightarrow \frac{v}{\Delta t_2} = 3A \cdot u_1 \rightarrow \Delta t_2 = \frac{v}{3A \cdot u_1}$$

$$\frac{\Delta t_2}{\Delta t_1} = \frac{\frac{v}{3A \cdot u_1}}{\frac{v}{A \cdot u_1}} \rightarrow \frac{\Delta t_2}{\Delta t_1} = \frac{1}{3} \quad (\text{iii})$$

B3. $u_1' = \frac{m_1 - m_2}{m_1 + m_2} \cdot u_1$

$$u_2' = \frac{2m_1}{m_1 + m_2} \cdot u_1$$

ΑΔΟ $\vec{p}_1 + \vec{p}_2 = \vec{p}_1' + \vec{p}_2'$

$$p_1 - \frac{p_1}{5} = \vec{p}_2' \rightarrow \vec{p}_2' = \frac{4p_1}{5}$$

$$\rightarrow m_2 \cdot u_2' = \frac{4}{5} \cdot m_1 \cdot u_1$$

$$\rightarrow m_2 \cdot \frac{2m_1}{m_1 + m_2} \cdot u_1 = \frac{4}{5} m_1 \cdot u_1$$

$$\rightarrow \frac{2m_1}{m_1 + m_2} = \frac{4}{5}$$

$$\rightarrow 10m_2 = 4m_1 + 4m_2$$

$$\rightarrow 6m_2 = 4m_1$$

$$\rightarrow 3m_2 = 2m_1 \rightarrow m_2 = \frac{2}{3}m_1$$

$$\left[u_2' = \frac{2m_1}{m_1 + \frac{2}{3}m_1} \cdot u_1 = \frac{2m_1}{\frac{5}{3}m_1} \cdot u_1 = \frac{4}{5}u_1 \right]$$

$$\frac{\Delta k_2}{k_1} \cdot 100\% = \frac{k'_2}{k_1} \cdot 100\% = \frac{\frac{1}{2} m_2 \cdot u_2'^2}{\frac{1}{2} m_1 \cdot u_1^2} \cdot 100\% = \frac{\frac{3}{2} m_2 \cdot \left(\frac{4}{5} u_1\right)^2}{\frac{1}{2} m_1 \cdot u_1^2} \cdot 100\%$$

$$= \frac{3 \cdot 16}{8 \cdot 25} \cdot 100\% = \frac{48}{50} \cdot 100\% = 96\% \quad (\text{iii})$$

ΘΕΜΑ Γ

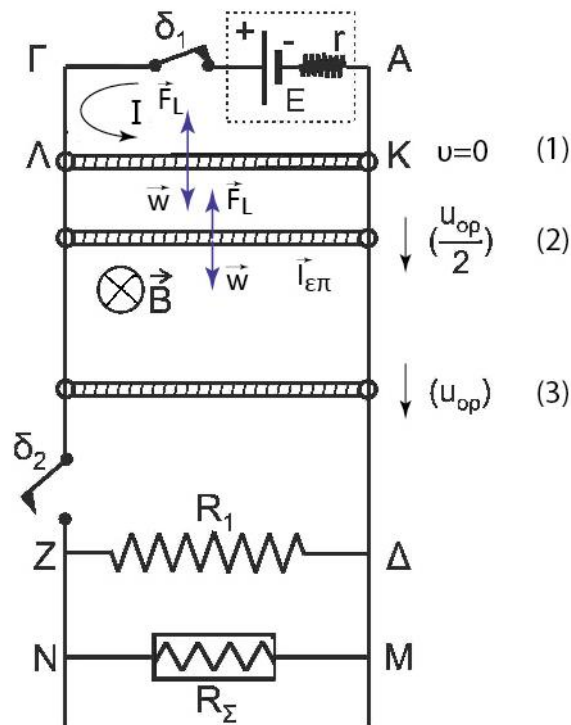
$\ell = 1 \text{ m}$

$\varepsilon = 9 \text{ V}$

$r = 1 \Omega$

$m = 0,3 \text{ kg}$

$R_{\text{κλ}} = 2 \Omega$



Γ1.

$$\left. \begin{aligned} \Sigma F = 0 \rightarrow F_L = w \rightarrow B l \ell = mg \\ I = \frac{\varepsilon}{R_{\text{κλ}} + r} = \frac{9}{3} = 3\text{A} \end{aligned} \right\} B = 1\text{T}$$

Γ2.

$$\left. \begin{aligned} R_1 = 3\Omega \\ v_{\text{κ}} = 6\text{V} \\ P_{\text{κ}} = 6\text{W} \end{aligned} \right\} P_{\text{κ}} = \frac{V_{\text{κ}}^2}{R_{\Sigma}} \rightarrow R_{\Sigma} = 6\Omega \left\{ \begin{aligned} R_{1,\Sigma} = \frac{R_1 \cdot R_{\Sigma}}{R_1 + R_{\Sigma}} = 2\Omega \end{aligned} \right.$$

$$\Sigma F = m \cdot \alpha \rightarrow w - F_L = m \cdot \alpha \rightarrow mg - B l \ell = m \alpha$$

$$\rightarrow mg - B \cdot \frac{\varepsilon_{\text{επ}}}{R_{\text{ολ}}} \cdot \ell = m \alpha$$

$$\rightarrow mg - B \cdot \frac{B u \ell}{R_{1,\Sigma} + R_{\text{κλ}}} \cdot \ell = m \alpha (*)$$

$$\rightarrow \alpha = g - \frac{B^2 \ell^2 \cdot u}{m(R_{1,\Sigma} + R_{\text{κλ}})}$$

$$\rightarrow \alpha = 10 - \frac{u}{0,3 \cdot 4} \rightarrow \alpha = 10 - \frac{5}{6} u \text{ (S.I.)}$$

$$(*) \text{ Στον (ΚΛ): } |\varepsilon_{\text{επ}}| = \left| \frac{\Delta \Phi}{\Delta t} \right| = \frac{B \ell \cdot \Delta x}{\Delta t} = B u \ell$$

$$\text{Συνεπώς } u \uparrow \rightarrow \alpha \downarrow \text{ μέχρι } \alpha = 0 \rightarrow \Sigma F = 0 \rightarrow u_{\text{ορ}} \text{ (σταθερή)}$$

$$\alpha = 10 - \alpha = 10 - \frac{5}{6} \cdot u \rightarrow 0 = 10 - \frac{5}{6} \cdot u_{\text{ορ}} \rightarrow u_{\text{ορ}} = 12\text{m/s}$$

Γ3.

$$I = \frac{\varepsilon_{\text{επ}}}{R_{\text{ολ}}} = \frac{B u \ell}{R_{1,\Sigma} + R_{\text{κλ}}} = \frac{B \frac{u_{\text{ορ}}}{2} \cdot \ell}{R_{1,\Sigma} + R_{\text{κλ}}} = \frac{6}{4} = 1,5\text{A}$$

$$\Sigma F = w - F_L \rightarrow \Sigma F = mg - B l \ell$$

$$\rightarrow \Sigma F = 3 - 1,5 \rightarrow \Sigma F = 1,5\text{N}$$

ή

$$\alpha = 10 - \frac{5}{6} \cdot \frac{u_{\text{ορ}}}{2} = 10 - \frac{5}{6} \cdot 6 = 5\text{m/s}^2$$

$$\frac{\Delta P}{\Delta t} = \Sigma F = m \cdot \alpha = 0,3 \cdot 5 = 1,5\text{N}$$

$$\Gamma 4. \quad I = \frac{\varepsilon_{\text{επ}}}{R_{\text{ολ}}} = \frac{Bv_{\text{οπ}} \ell}{R_{1,\Sigma} + R_{\text{κλ}}} = \frac{12}{4} = 3\text{A}$$

$$V_{\text{MN}} = I \cdot R_{1,\Sigma} = 3 - 2 = 6\text{V} = V_{\text{κ}}$$

Λειτουργεί κανονικά.

ΘΕΜΑ Δ

$$M_p = 3\text{kg}$$

$$\ell = 2\text{m}$$

$$m = 1\text{kg}$$

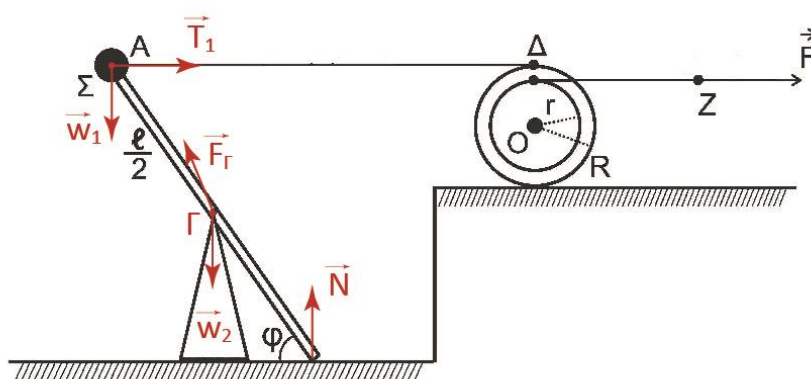
$$\eta\mu\phi = 0,8$$

$$\sigma\upsilon\nu\phi = 0,6$$

$$M_T = 7\text{kg}$$

$$R = 0,4\text{m}$$

$$r = 0,3\text{m}$$



Δ1.

$$T_1 = 10,5\text{N}$$

$$N = ?$$

$$\Sigma\tau^{(r)} = 0 \rightarrow N \cdot \frac{\ell}{2} \sigma\upsilon\nu\phi + w_1 \cdot \frac{\ell}{2} \sigma\upsilon\nu\phi - T_1 \cdot \frac{\ell}{2} \eta\mu\phi = 0$$

$$\rightarrow N \cdot 0,6 + 10 \cdot 0,6 - 10,5 \cdot 0,8 = 0$$

$$\rightarrow N + 10 - \frac{4}{3} 10,5 = 0$$

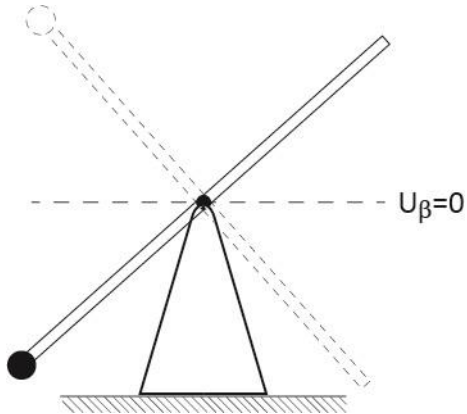
$$\rightarrow N = 14 - 10 \rightarrow N = 4\text{N}$$

$$\Delta 2. \quad \Sigma\tau = I_{\text{ολ}} \cdot \alpha_{\gamma\omega\nu} \rightarrow w_1 \cdot \frac{\ell}{2} \sigma\upsilon\nu\phi = I_{\text{ολ}} \cdot \alpha_{\gamma\omega\nu}$$

$$\rightarrow \alpha_{\gamma\omega\nu} = 3\text{rad/s}^2$$

$$\frac{dL}{dt} \rho = \Sigma\tau_p = I_p^{(r)} \cdot \alpha_{\gamma\omega\nu} = \frac{1}{12} M\rho\ell^2 \cdot \alpha_{\gamma\omega\nu} = 1 \cdot 3 = 3\text{kg m}^2/\text{s}^2$$

Δ3.



$$I_{ολ} = \frac{1}{12} M \rho \ell^2 + m \left(\frac{\ell}{2} \right)^2 = \frac{1}{12} \cdot 3 \cdot 4 + 1 \cdot 1^2 = 1 + 1 = 2 \text{ kg m}^2$$

ΑΔΜΕ I → II $k_I + U_I = k_{II} + U_{II}$

$$m_1 g \frac{\ell}{2} \eta \mu \phi = \frac{1}{2} I_{ολ} \omega^2 - m_1 g \frac{\ell}{2}$$

$$m_1 g \ell \eta \mu \phi = \frac{1}{2} I_{ολ} \omega^2 \rightarrow 16 = \omega^2 \rightarrow 4 \text{ rad/s}$$

$$L_{αρχ} = I_{ολ} \cdot \omega = 2 \cdot 4 = 8 \text{ kg m}^2 / \text{s}$$

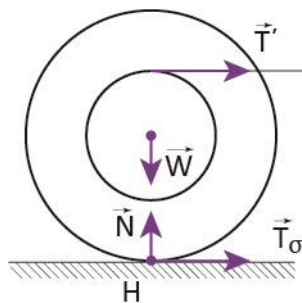
$$L_{τελ} = I_{ολ} \cdot \frac{\omega}{2} = 2 \cdot 2 = 4 \text{ kg m}^2 / \text{s}$$

$$\vec{L}_{τελ} \quad \vec{L}_{αρχ} \quad \vec{\Delta L} = \vec{L}_{τελ} - \vec{L}_{αρχ}$$

$$\odot \quad \otimes \quad \Delta L = L_{τελ} - (-L_{αρχ})$$

$$\vec{\Delta L} \otimes \quad \Delta L = L_{τελ} + L_{αρχ} = 12 \text{ kg m}^2 / \text{s}$$

Δ4.



$$F = T = T' = 12\text{N}$$

Στο σημείο Η

$$v_H = v_{cm} - v_{yp}$$

$$v_{cm} = v_{yp} = \omega \cdot R \rightarrow \alpha_{cm} = \alpha_{\gamma\omega\nu} R$$

$$\begin{aligned} \Sigma F_x = M_T \cdot \alpha_{cm} &\rightarrow T' + T\sigma = M_T \cdot \alpha_{cm} \\ &\rightarrow F + T\sigma = M_T \cdot \alpha_{cm} \quad (1) \end{aligned}$$

$$\begin{aligned} \Sigma \tau = I_{cm(T)} \cdot \alpha_{\gamma\omega\nu} &\rightarrow T' \cdot r - T\sigma \cdot R = \frac{1}{2} M_T \cdot R^2 \cdot \frac{\alpha_{cm}}{R} \\ &\rightarrow F \cdot \frac{3}{4} - T\sigma = \frac{1}{2} M_T \cdot \alpha_{cm} \quad (2) \end{aligned}$$

$$\xrightarrow{(1)+(2)} F + \frac{3}{4}F = \frac{3}{4}M_T \cdot \alpha_{cm} \rightarrow 21 = \frac{3}{2} \cdot 7 \cdot \alpha_{cm} \rightarrow \alpha_{cm} = 2\text{m/s}^2$$

Δ5.

$$\alpha_{\gamma\omega\nu} = \frac{\alpha_{cm}}{R} = \frac{2}{0,4} = 5\text{ rad/s}^2$$

$$\Delta x_{\gamma\omega\nu} = \frac{1}{2} \alpha_{cm} \cdot t^2 = \frac{1}{2} \cdot 2 \cdot 2^2 = 4\text{m}$$

$$\Delta \phi = \frac{1}{2} \alpha_{\gamma\omega\nu} t^2 = \frac{1}{2} \cdot 5 \cdot 2^2 = 10\text{rad}$$

$$\begin{aligned} W_f &= F \cdot \Delta x_{cm} + Z_f \cdot \Delta \phi \\ &= F \cdot \Delta x_{cm} + F \cdot r \cdot \Delta \phi \\ &= 12 \cdot 4 + 12 \cdot 0,3 \cdot 10 \\ &= 48 + 36 \\ &= 84\text{J} \end{aligned}$$

ΚΑΛΑ ΑΠΟΤΕΛΕΣΜΑΤΑ!!!